CLAIMS

1. A cryptographic system combining the socalled discrete logarithm and factorization principles, comprising, among other things, public keys and a secret key, characterised in that the said public keys comprise, at least:

a. an RSA modulus n, greater in size than 640bits, having the following property:

$$n = (A p_A + 1) \times (B p_B + 1)$$

in_which:

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 p_{A} and p_{B} are prime numbers greater in size than 320 bits,

 $(A p_A + 1)$ is an RSA prime denoted p,

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 $(B p_B + 1)$ is an RSA prime denoted q,

A is the product of k/2 (k being an even integer number between 10 and 120) prime numbers (denoted p[i], i = 1 to k/2) of relatively small size (between 2 and 16 bits) and

B is the product of k/2 prime numbers (also denoted p[i], i = k/2 + 1 to k);

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the p[i]s being of relatively small size (between 2 and 16 bits), and also able to be mutually prime;

- b. an exponentiation base g, of order $\phi(n)/4$ (where $\phi(n)$ denotes the Euler indicator function), g therefore having not to be a p[i]-th power modulo n of any number.
- 2. A cryptographic system according to Claim 1 comprising at least an encryption/decryption system 1, characterised in that the encryption of a message m, m < AB, consists of the operation:

 $c = q^m \mod n$

where c denotes the cryptogram (encrypted 15 message).

- 3. A cryptographic system according to Claim 2 comprising an encryption/decryption system, characterised in that the integrity of m can be provided by the encryption of m|h(m) (h denoting a hashing function and | denoting concatenation), or by the encryption of DES(key, m), the said key being a key accessible to all.
- 25 4. A cryptographic system according to Claim 1 comprising an encryption/decryption system and a key escrow system, characterised in that:
 - the said secret key of the decrypter or of the escrow centre is the number $\phi(n)$, and in that the operation of decryption or of recovering the identity of a user consists of the following steps:

- a. calculating, for i from 1 to k: $y[i] = C^{\phi(n)/p[i]} \mod n$;
- b. for i from 1 to k
 for j from 1 to p[i]

comparing y[i] with the values $g^{j\phi(n)/p\{i\}}$ mod n independent of m;

if $g^{j\phi(n)/p\{i\}}$ mod n = y[i] then assign $\mu[i] =$

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- c. reconstructing the message m from the Chinese remainder theorem CRT and the values $\mu \left[\text{i} \right].$
- or 5 comprising an encryption/decryption system and a key escrow system, characterised in that the said decrypter speeds up the calculation of the quantities y[i] by calculating:

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- a) $z = c^r \mod n$ where $r = p_A p_B$
- b) for i from 1 to k: $y[i] = z^{AB/p[i]} \mod n$,
- 25 so as to take advantage of the difference in size between AB/p[i] and $\phi(n)/p[i]$ for speeding up the calculations.
- 6. A cryptographic system according to Claim 4 comprising an encryption/decryption system and a key escrow system or 5, characterised in that the decrypter pre-calculates and saves, once and for all, the table of values $g^{j\phi(n)/p[i]}$ mod n for $1 \le i \le k$ and $1 \le j \le p[i]$

or,

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more specifically, a truncation or a hashing of these values (denoted h) having the following property:

 $h(g^{j\phi(n)/p[i]} \mod n) \neq h(g^{j'\phi(n)/p[i]} \mod n) \text{ if } j \neq j'.$

- 7. A cryptographic system according to any one 10 of Claim 4 to 6 comprising an encryption/decryption system and a key escrow system, characterised in that the decrypter speeds up its calculations by separately decrypting the message modulo p and then modulo q, and constructing the modulo results with the help of the Chinese remainder theorem in order to find magain.
- 8. A cryptographic system according to any one
 20 of Claims 4 to 7, characterised in that a key
 escrow centre or authority implements the
 following steps:
 - a. it codes the identity of the user ID = Σ 2ⁱ⁻¹ ID[i] where ID[i] are the bits of the identity of the said user of the system (the sum being taken for i from 1 to k) by calculating e(ID) = Π p[i]^{ID[i]} (the product being taken for i from 1 to k);

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b. it issues, to the user, an El-Gamal key (that is to say an exponentiation base) $c = q^{e(ID)u} \mod n$,

in which u is a large random prime or a number prime with $\phi(n)$;

- c. it thus makes it possible for the user to derive, from c, his El-Gamal public key by choosing a random number x and raising c to the power x modulo n.
- d. with the aim of finding the trace of the user, the authority extracts, from the El-Gamal cryptogram of the encrypter, the said cryptogram always comprising two parts, the part:

 $v = c^r \mod n$

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where r is the encryption random number chosen by the encrypter.

- e. Knowing $\phi(n)$, the said authority finds the 20 bits ID[i] by means of the following algorithm:
 - 1. calculate, for i from 1 to k: $y[i] = v^{\phi(n)/p[i]} \mod n$
- - 3. calculate:

4. find : ID = CCE(ID')

in which CCE denotes an error correction 35 mechanism.

9. A cryptographic system according to any one of Claims 4 to 7 comprising a key escrow system, characterised in that it is based on the so-called Diffie-Hellman key exchange mechanism where a number c, obtained by raising g to a random power a modulo n by one of the parties, is intercepted by the said escrow authority:

 $c = g^a \mod n$

the said escrow authority finds a again in the following manner:

15 a. knowing the factorization of n, the said authority finds, with the help of the decryption algorithm, the value

 $\alpha = a \mod AB$

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that is $a = \alpha + \beta AB$;

b. the said authority calculates: $\lambda = c/g^{\alpha} \mod n = g^{\beta AB} \mod n$

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c. using a cryptanalysis algorithm, the authority calculates the discrete logarithm $\boldsymbol{\beta}$

 $\lambda = (q^{AB})^{\beta} \mod n$

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d. the authority finds

 $a = \alpha + \beta AB$

and decrypts the communications based on the use of a.

- 10. A cryptographic system according to any one of Claims 2 to 9 comprising an encryption/decryption system and a key escrow system, characterised in that the RSA modulus n is the product of three factors:
- 10 $n = (Ap_A + 1) \times (Bp_B + 1) \times (Cp_C + 1)$

in which P_A , P_B , P_C are prime numbers greater in size than 320 bits,

- 15 $(Ap_A + 1)$, $(Bp_B + 1)$, $(Cp_C + 1)$ are RSA primes, denoted respectively p, q, r,
- A, B and C are each the product of k/3 prime numbers (denoted p[i], i = 1 to k), the p[i]s 20 being of relatively small size (between 2 and 16 bits) and able to be mutually prime numbers and k being an integer number between 10 and 120, so that the product ABC has at least 160 bits.
- 11. A cryptographic system according to any one 25 of Claims 10 comprising 1 to encryption/decryption or escrow system, characterised in that the items of encryption, key escrow equipment decryption and computers, chip cards, PCMCIA cards, badges, 30 or any other portable contactless cards equipment.
- 12. A device comprising a cryptographic system
 35 according to any one of the preceding claims,
 characterised in that it comprises an encryption

system and/or a decryption system and/or a key escrow system, the said systems communicating with one another by an exchange of electronic signals or by means of an exchange of radio waves or infrared signals.